



Categories and General Algebraic Structures with Applications

Volume 12, Number 1, January 2020
ISSN Print: 2345-5853 Online: 2345-5861



Shahid Beheshti University
<http://cgasa.sbu.ac.ir>

In the Name of God

Categories and General Algebraic Structures

with Applications

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Publisher: Shahid Beheshti University.

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