



Categories and  
**General Algebraic Structures**  
with Applications

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In the Name of God

# Categories and General Algebraic Structures

## with Applications

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**Robert Paré**, Department of Mathematics and Statistics, Dalhousie University, 6316 Coburg Road, Halifax, Nova Scotia, Canada B3H 3J5, *pare@mathstat.dal.ca*.

**Jorge Picado**, Department of Mathematics, University of Coimbra, Apartado 3008, 3001-454, Coimbra, Portugal, [picado@mat.uc.pt](mailto:picado@mat.uc.pt).

**Andrew Pitts**, Computer Laboratory, University of Cambridge, William Gates Building, 15 JJ Thomson Avenue, Cambridge CB3 0FD, United Kingdom, [andrew.pitts@cl.cam.ac.uk](mailto:andrew.pitts@cl.cam.ac.uk).

**Masoud Pourmahdian**, Department of Mathematics and Computer Sciences, Amirkabir University of Technology, Tehran, Iran; School of Mathematics, Institute for Research in Fundamental Sciences (IPM), P.O. Box 19395-5746, Tehran, Iran, [pourmahd@ipm.ir](mailto:pourmahd@ipm.ir).

**Jim Renshaw**, School of Mathematics, University of Southampton, Highfield, Southampton, SO17 1BJ, United Kingdom, [j.h.renshaw@maths.soton.ac.uk](mailto:j.h.renshaw@maths.soton.ac.uk).

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**Gavin J. Seal**, Mathematics Section, Ecole Polytechnique Federale de Lausanne (EPFL), GH-1015 Lausanne, Switzerland, [gavin.seal@epfl.ch](mailto:gavin.seal@epfl.ch).

**Omid Ali Shahni Karamzadeh**, Department of Mathematics, Shahid Chamran University, Ahvaz, Iran, [karamzadeh@cua.ac.ir](mailto:karamzadeh@cua.ac.ir).

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**Walter Tholen**, Department of Mathematics and Statistics, York University, Toronto, Ontario M3J 1P3, Canada, [tholen@mathstat.yorku.ca](mailto:tholen@mathstat.yorku.ca).

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