



Categories and General Algebraic Structures with Applications

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In the Name of God

Categories and General Algebraic Structures

with Applications

Editor-in-Chief:
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Piergiulio Corsini, Department of Civil Engineering and Architecture, Via delle Scienze 208, 33100 Udine, Italy, *piergiulio.corsini@uniud.it*.

Brian A. Davey, Department of Mathematics and Statistics, La Trobe University, Bundoora (Melbourne) VIC 3083, Australia, *b.davey@latrobe.edu.au*.

Dikran Dikranjan, Department of Mathematics and Computer Science, University of Udine, Via delle Scienze, 208 – Loc. Rizzi, 33100 Udine, Italy, *dikranjan@dimi.uniud.it*.

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- Ali Iranmanesh**, Department of Mathematics, Tarbiat Modares University, P.O. Box 14115-137, Tehran, Iran, *iranmana@modares.ac.ir*.
- George Janelidze**, Department of Mathematics and Applied Mathematics, University of Cape Town, Private Bag, Rondebosch, 7701, South Africa, *janelg@telkomsa.net*.
- Peter T. Johnstone**, Department of Pure Mathematics and Mathematical Statistics, Centre for Mathematical Sciences, University of Cambridge, Wilberforce Road, Cambridge CB3 0WB, United Kingdom, *p.t.johnstone@dpmms.cam.ac.uk*.
- Vinayak Joshi**, Department of Mathematics, University of Pune, Ganeshkhind, Pune, Maharashtra 411007, India, *vvj@math.unipune.ac.in*.
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- Achim Jung**, School of Computer Science, The University of Birmingham, Edgbaston, Birmingham, B15 2TT, United Kingdom, *a.jung@cs.bham.ac.uk*.
- Bakhadyr Khoussainov**, Department of Computer Science, University of Auckland, Private Bag 92019, Auckland, New Zealand, *bmk@cs.auckland.ac.nz*.
- Mati Kilp**, Institute of Pure Mathematics, University of Tartu, 50409 Tartu, Estonia, *mk-ilp@math.ut.ee*.
- Ulrich Knauer**, Institut für Mathematik, Carl von Ossietzky Universität Oldenburg, D-26111 Oldenburg, Germany, *knauer@mathematik.uni-oldenburg.de*.
- Valdis Laan**, Institute of Pure Mathematics, University of Tartu, 50409 Tartu, Estonia, *vlaan@ut.ee*.
- Jorge Martinez**, Department of Mathematics, University of Florida, Gainesville, FL 32611-8105, United States of America, *martinbad@ufl.edu*.
- M. Andrew Moshier**, Department of Mathematics and Computation, Faculty of Mathematics, Physics and Computation, Schmid College of Science and Technology, Chapman University, Orange, CA 92866, United States of America, *moshier@chapman.edu*.
- Peeter Normak**, Institute of Informatics, Tallinn University, Narva Road 25, Tallinn 10120, Estonia, *peeter.normak@tlu.ee*.
- Robert Paré**, Department of Mathematics and Statistics, Dalhousie University, 6316 Coburg Road, Halifax, Nova Scotia, Canada B3H 3J5, *pare@mathstat.dal.ca*.
- Jorge Picado**, Department of Mathematics, University of Coimbra, Apartado 3008, 3001-454, Coimbra, Portugal, *picado@mat.uc.pt*.
- Andrew Pitts**, Computer Laboratory, University of Cambridge, William Gates Building, 15 JJ Thomson Avenue, Cambridge CB3 0FD, United Kingdom, *andrew.pitts@cl.cam.ac.uk*.

Masoud Pourmahdian, Department of Mathematics and Computer Sciences, Amirkabir University of Technology, Tehran, Iran; School of Mathematics, Institute for Research in Fundamental Sciences (IPM), P.O. Box 19395-5746, Tehran, Iran, *pourmahd@ipm.ir*.

Jim Renshaw, School of Mathematics, University of Southampton, Highfield, Southampton, SO17 1BJ, United Kingdom, *j.h.renshaw@maths.soton.ac.uk*.

Jan Rutten, Faculty of Science, Radboud University, Comeniuslaan 4, 6525 HP Nijmegen, The Netherlands, *jan.rutten@cwi.nl*.

Hanamantagouda P. Sankappanavar, Department of Mathematics, State University of New York, New Paltz, New York 12561, United States of America, *sankapph@hawkmail.newpaltz.edu*.

Gavin J. Seal, Mathematics Section, Ecole Polytechnique Federale de Lausanne (EPFL), GH-1015 Lausanne, Switzerland, *gavin.seal@epfl.ch*.

Omid Ali Shahni Karamzadeh, Department of Mathematics, Shahid Chamran University, Ahvaz, Iran, *karamzadeh@cua.ac.ir*.

Kunitaka Shoji, Department of Mathematics, Shimane University, Matsue, Shima 690, Japan, *ksho@riko.shimane-u.ac.jp*.

Manuela Sobral, Department of Mathematics, University of Coimbra, Apartado 3008, 3001-454, Coimbra, Portugal, *sobral@mat.uc.pt*.

Andrzej Tarlecki, Faculty of Mathematics, Informatics, and Mechanics, Institute of Informatics, University of Warsaw, Banacha 2, 02-097 Warszawa, Poland, *a.tarlecki@mimuw.edu.pl*.

Walter Tholen, Department of Mathematics and Statistics, York University, Toronto, Ontario M3J 1P3, Canada, *tholen@mathstat.yorku.ca*.

Aims and Scope:

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