



Categories and General Algebraic Structures with Applications

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Dedicated to Prof. Themba Dube (II)



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In the Name of God

Categories and General Algebraic Structures with Applications

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Piergiulio Corsini, Department of Civil Engineering and Architecture, Via delle Scienze 208,

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Brian A. Davey, Department of Mathematics and Statistics, La Trobe University, Bundoora (Melbourne) VIC 3083, Australia, *b.davey@latrobe.edu.au*.

Dikran Dikranjan, Department of Mathematics and Computer Science, University of Udine, Via delle Scienze, 208 – Loc. Rizzi, 33100 Udine, Italy, *dikranjan@dimi.uniud.it*.

Abbas Edalat, Department of Computing, Imperial College London, 180 Queen’s Gate, London SW7 2RH, United Kingdom, *a.edalat@imperial.ac.uk*.

Majid Ershad, Department of Mathematics, Shiraz University, Shiraz, Iran, *ershad@shirazu.ac.ir*.

Christopher Gilmour, Department of Mathematics and Applied Mathematics, University of Cape Town, Private Bag, Rondebosch, 7701, South Africa, *christopher.gilmour@uct.ac.za*.

Eraldo Giuli, Dipartimento di Matematica Pura ed Applicata, Università di L’Aquila, Coppito 67010, L’Aquila, Italy, *giuli@univaq.it*.

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Marco Grandis, Dipartimento di Matematica, Università di Genova, Via Dodecaneso 35, 16146 Genova, Italy, *grandis@dimma.unige.it*.

Hossein Hajibolhassan, Department of Mathematics, Faculty of Mathematical Sciences, Shahid Beheshti University, Evin 19839, Tehran, Iran, *hhaji@sbu.ac.ir*.

Wei He, School of Mathematical Sciences, Nanjing Normal University, China, *weihe@njnu.edu.cn*.

Dirk Hofmann, Departamento de Matemática, Universidade de Aveiro, 3810-193 Aveiro, Portugal, *dirk@ua.pt*.

Martin Hyland, Department of Pure Mathematics and Mathematical Statistics, Centre for Mathematical Sciences, University of Cambridge, Wilberforce Road, Cambridge CB3 0WB, United Kingdom, *m.hyland@dpmms.cam.ac.uk*.

Ali Iranmanesh, Department of Mathematics, Tarbiat Modares University, P.O. Box 14115-137, Tehran, Iran, *iranmana@modares.ac.ir*.

George Janelidze, Department of Mathematics and Applied Mathematics, University of Cape Town, Private Bag, Rondebosch, 7701, South Africa, *janelg@telkomsa.net*.

Peter T. Johnstone, Department of Pure Mathematics and Mathematical Statistics, Centre for Mathematical Sciences, University of Cambridge, Wilberforce Road, Cambridge CB3 0WB, United Kingdom, *p.t.johnstone@dpmms.cam.ac.uk*.

Vinayak Joshi, Department of Mathematics, University of Pune, Ganeshkhind, Pune, Maharashtra 411007, India, *vvj@math.unipune.ac.in*.

André Joyal, Département de Mathématiques, Université du Québec à Montréal, C.P. 8888, Succ. Centre-ville Montréal, QC H3C 3P8, Canada, *joyal.andre@uqam.ca*.

Achim Jung, School of Computer Science, The University of Birmingham, Edgbaston, Birmingham, B15 2TT, United Kingdom, *a.jung@cs.bham.ac.uk*.

Bakhadyr Khossainov, Department of Computer Science, University of Auckland, Private Bag 92019, Auckland, New Zealand, *bmk@cs.auckland.ac.nz*.

Mati Kilp, Institute of Pure Mathematics, University of Tartu, 50409 Tartu, Estonia, *mkilp@math.ut.ee*.

Ulrich Knauer, Institut für Mathematik, Carl von Ossietzky Universität Oldenburg, D-26111 Oldenburg, Germany, *knauer@mathematik.uni-oldenburg.de*.

Valdis Laan, Institute of Pure Mathematics, University of Tartu, 50409 Tartu, Estonia, *vlaan@ut.ee*.

Jorge Martinez, Department of Mathematics, University of Florida, Gainesville, FL 32611-8105, United States of America, *martinbad@ufl.edu*.

M. Andrew Moshier, Department of Mathematics and Computation, Faculty of Mathematics, Physics and Computation, Schmid College of Science and Technology, Chapman University, Orange, CA 92866, United State of America, *moshier@chapman.edu*.

Peeter Normak, Institute of Informatics, Tallinn University, Narva Road 25, Tallinn 10120, Estonia, *peeter.normak@tlu.ee*.

Robert Paré, Department of Mathematics and Statistics, Dalhousie University, 6316 Coburg

Road, Halifax, Nova Scotia, Canada B3H 3J5, pare@mathstat.dal.ca.

Jorge Picado, Department of Mathematics, University of Coimbra, Apartado 3008, 3001-454, Coimbra, Portugal, picado@mat.uc.pt.

Andrew Pitts, Computer Laboratory, University of Cambridge, William Gates Building, 15 JJ Thomson Avenue, Cambridge CB3 0FD, United Kingdom, andrew.pitts@cl.cam.ac.uk.

Masoud Pourmahdian, Department of Mathematics and Computer Sciences, Amirkabir University of Technology, Tehran, Iran; School of Mathematics, Institute for Research in Fundamental Sciences (IPM), P.O. Box 19395-5746, Tehran, Iran, pourmahd@ipm.ir.

Jim Renshaw, School of Mathematics, University of Southampton, Highfield, Southampton, SO17 1BJ, United Kingdom, j.h.renshaw@maths.soton.ac.uk.

Jan Rutten, Faculty of Science, Radboud University, Comeniuslaan 4, 6525 HP Nijmegen, The Netherlands, jan.rutten@cwi.nl.

Hanamantagouda P. Sankappanavar, Department of Mathematics, State University of New York, New Paltz, New York 12561, United States of America, sankapph@hawkmil.newpaltz.edu.

Gavin J. Seal, Mathematics Section, Ecole Polytechnique Federale de Lausanne (EPFL), GH-1015 Lausanne, Switzerland, gavin.seal@epfl.ch.

Omid Ali Shahni Karamzadeh, Department of Mathematics, Shahid Chamran University, Ahvaz, Iran, karamzadeh@cua.ac.ir.

Kunitaka Shoji, Department of Mathematics, Shimane University, Matsue, Shima 690, Japan, ksho@riko.shimane-u.ac.jp.

Manuela Sobral, Department of Mathematics, University of Coimbra, Apartado 3008, 3001-454, Coimbra, Portugal, sobral@mat.uc.pt.

Andrzej Tarlecki, Faculty of Mathematics, Informatics, and Mechanics, Institute of Informatics, University of Warsaw, Banacha 2, 02-097 Warszawa, Poland, a.tarlecki@mimuw.edu.pl.

Walter Tholen, Department of Mathematics and Statistics, York University, Toronto, Ontario M3J 1P3, Canada, tholen@mathstat.yorku.ca.

Aims and Scope:

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