

Categories and General Algebraic Structures with Applications

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Dedicated to Professor George A. Grätzer





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Categories and

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Aims and Scope:

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Contents

G. Czédli	
Celebrating Professor George A. Grätzer	1
Gábor Czédli	
An interview with George A. Grätzer	11
Bernhard Banaschewski	
The function ring functors of pointfree topology revisited	19
A. Ilaghi-Hosseini, S.Sh. Mousavi, and S.N. Hosseini	
On Semi Weak Factorization Structures	33
G. Czédli and Á. Kurusa	
A convex combinatorial property of compact sets in the plane and its roots in lattice theory	57
A. Karimi Feizabadi	
The categories of lattice-valued maps, Equalities, Free objects, and $\mathcal{C}\text{-reticulation}$	93
D. Baboolal, J. Picado, and A. Pultr	
Another proof of Banaschewski's surjection theorem	113
A. Delfan, H. Rasouli, and A. Tehranian	

3	3	Jо	nt	en	ts	
		20	110	CII	. UD	

Intersection graphs associated with semigroup acts	131	
G.M. Bergman		
Completeness results for metrized rings and lattices	149	
M. Haddadi and S.M.N. Sheykholislami		
(r,t)-injectivity in the category S-Act	169	
V. Joshi and B.N. Waphare		
Frankl's Conjecture for a subclass of semimodular lattices	197	