

# Categories and General Algebraic Structures with Applications

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## $\begin{array}{c} {\bf Categories \ and} \\ {\bf General \ Algebraic \ Structures} \end{array}$

#### with **Applications**

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#### Aims and Scope:

"Categories and General Algebraic Structures with Applications" is an international journal published by Shahid Beheshti University, Tehran, Iran, free of page charges. It publishes original high quality research papers and invited research and survey articles mainly in two subjects: Categories (algebraic, topological, and applications in mathematics and computer sciences) and General Algebraic Structures (not necessarily classical algebraic structures, but universal algebras such as algebras in categories, semigroups, their actions, automata, ordered algebraic structures, lattices (of any kind), quasigroups, hyper universal algebras, and their applications).

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