



Categories and
General Algebraic Structures
with Applications

Volume 6, Number 1, January 2017
ISSN Print: 2345-5853 Online: 2345-5861

Dedicated to Bernhard Banaschewski on the Occasion of his 90th Birthday (I)



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In the Name of God

Categories and General Algebraic Structures

with Applications

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Publisher: Shahid Beheshti University.

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